

Loop Quasi-Invariant Peeling

A method to optimize programs

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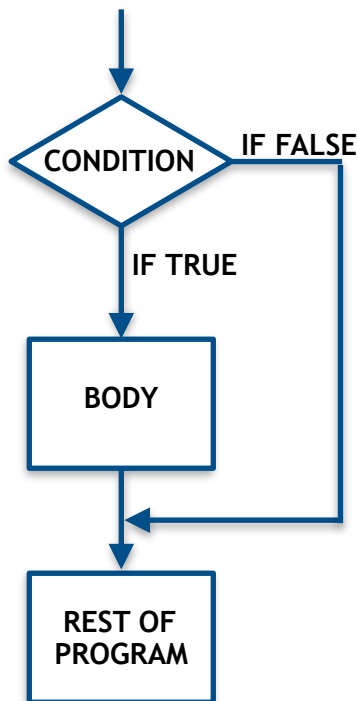
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Programs

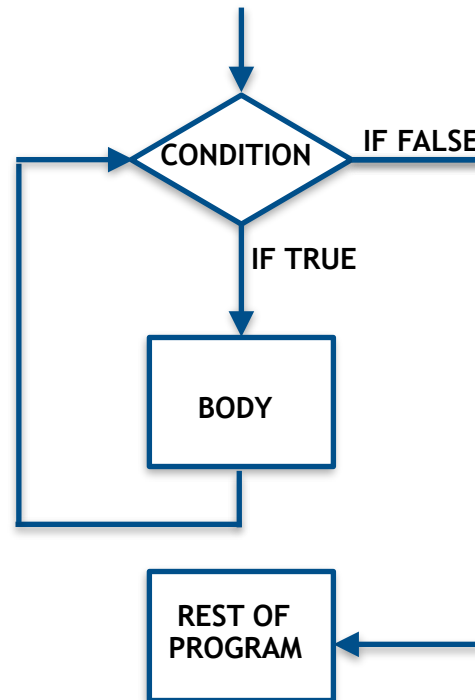
- Programs = set of instructions to perform a task
- Types of instructions:
 - Data modification
 - Control flow

Control-flow Instructions

If...else...



Loops: while, do...while, for



Programming Language

```
for i in batch {  
  oven.preheat()  
  bowl.add(dry_ingredients)  
  bowl.mix()  
  ....  
  cookies.bake()  
}
```



Machine Language

```
00000000 0000 0001 0001  
00000100 0000 0016 0000  
00000200 0000 0001 0004  
00000300 0000 0000 0000  
00000400 0004 8384 0084  
00000500 00e9 6a69 0069  
00000600 00fc 1819 0019  
00000700 0057 7b7a 007a  
00000800 8888 8888 8888  
00000900 3b83 5788 8888  
00000a00 d61f 7abd 8818  
00000b00 8b06 e8f7 88aa  
00000c00 8a18 880c e841  
00000d00 a948 5862 5884  
00000e00 3d86 dcb8 5cbb  
00000f00 8888 8888 8888  
00001000 0000 0000 0000
```

Example: Optimize Baking Time

For each batch:

Preheat oven

Mix dry stuff ...

Example: Optimize Baking Time

For each batch:
Preheat oven
Mix dry stuff ...

peel unnecessary
instruction



Preheat oven
For each batch:
Preheat oven
Mix dry stuff...

Loop Invariant Code Motion (LICM)

- Peeling: move commands that do not change within the loop to occur *before* the loop

```
i = 0;
while (i < n) {
    w = 20;
    x = y + z;
    i++;
}
```

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while (i < n) {  
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}
```


Proof of Equivalence

- Guarantee the optimized program performs the same tasks as the original

INPUT

Performs specified task(s)
Runs at a slower speed

OUTPUT

Performs specified task(s)
Runs at a faster speed

Algorithm Definition

Definition 6. Let $C := \text{while } E \text{ do } [C_1; C_2; \dots, C_n]$ be a command. We define the directed graph $\text{Dep}(C)$ as follows:

- the set of vertices $V^{\text{Dep}(C)}$ is equal to $\{C_1, \dots, C_n\}$ (the set of commands in the loop);
- the set of edges $E^{\text{Dep}(C)}$ is equal to $\uplus_{m=1}^n \uplus_{i \in \text{In}(C_m)} \text{PrD}_i(C_m)$ (the set of all principal dependencies);
- the source $s(i)$ of the edge $C_k \in \text{PrD}_i(C_m)$ is C_k ;
- the target $t(i)$ of the edge $C_k \in \text{PrD}_i(C_m)$ is C_m .

The *invariance degree* $\text{deg}_C(C_m)$ of a command C_m w.r.t. C is then defined as follows. When clear, we will avoid writing the subscript C to ease notations. If C_m is a source in $\text{Dep}(C)$, then $\text{deg}(C_m) = 1$. If C_m has a reflective edge in $\text{Dep}(C)$, then $\text{deg}(C_m) = \infty$. Otherwise, we write $\text{Fib}(C_m)$ – the *fiber* over C_m – the set of vertices in $\text{Dep}(C)$ defined as $\{C_k \mid \exists e \in E^{\text{Dep}(C)}, s(e) = C_k, t(e) = C_m\}$, and define $\text{deg}(C_m)$ by the following equation, where $\chi_{>m}(i) = 1$ if $i > m$ and $\chi_{>m}(i) = 0$ otherwise:

$$\text{deg}(C_m) = \max(\{\text{deg}(C_i) + \chi_{>m}(i) \mid C_i \in \text{Fib}(C_m)\})$$

In particular, if C_m is part of a cycle in $\text{Dep}(C)$, its degree is equal to ∞ .

For all $i \in \mathbf{N} \cup \{\infty\}$, we define the inverse image $\text{deg}^{-1}(i)$, i.e. $\text{deg}^{-1}(i) = \{C_k \mid \text{deg}(C_k) = i\}$, and we note $\text{maxdeg}(C)$ the largest integer (i.e. not equal to ∞) such that $\text{deg}^{-1}(\text{maxdeg}(C)) \neq \emptyset$. The following lemma will be used in the proof of the main theorem.

Algorithm Snippet

```
def comput_deg(tabDeg,i,lldep):
    if tabDeg[i]==0: // if deg(Ci) has not been computed
        if(len(lldep[i])==0): // if Ci has no dependencies, set deg(Ci) in tabDeg to 1
            tabDeg[i]=1
        else: //else compute max degree of Ci's dependencies(Cl)
            tabDeg[i]=-1
            deg=-1
            for l in lldep[i]:
                // compute degree for each dependency and update tabDeg
                tabDeg[l] = comput_deg(tabDeg,l,lldep)
                // if Ci is also a dependency of Cl, then there is a loop
                if tabDeg[l]==-1: return -1
                // if deg(Cl) is the max and Cl precedes Ci
                if (tabDeg[l]>deg) and l<i: deg=tabDeg[l]
                // if deg(Cl) is the max if Cl follows Ci
                if (tabDeg[l]>=deg) and l>i: deg=tabDeg[l]+1
                // do nothing if the current degree is the max
            tabDeg[i]=deg // set deg(Ci) in tabDeg to max degree
    return tabDeg[i]
```

Application

- Simplification
- Automatically generated
- No conflict

Results

- Improve original implementation
- Added tests
- Overall goal = transform

Limitations

- Proof of concept:
 - Programming language = C
 - Only certain types of instructions
 - Rest are ignored

Future work

- Add optimization to compiler
- Parallelization: split loops to run simultaneously

```
i = 0, j = 10, k = 0;
while (i < n) {
    j=j-1;
    k=k+1;
    i=i+1;
}
```



```
i = 0, j = 10, k = 0;
while (i < n) {
    j=j-1;
    i=i+1;
}

while (i < n) {
    k=k+1;
    i=i+1;
}
```

Conclusion

- Method for removing unnecessary instruction from loops

Thank you!